Ionospheric effects of whistler waves from rocket-triggered lightning

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Lightning-induced electron precipitation (LEP) is one of the primary mechanisms for energetic electron loss from Earth’s radiation belts. While previous works have emphasized lightning location and the return stroke peak current in quantifying lightning’s role in radiation belt electron loss, the spectrum of the lightning return stroke has received far less attention. Rocket-triggered lightning experiments performed at the International Center for Lightning Research and Testing (ICLRT) at Camp Blanding, Florida, provide a means to directly measure the spectral content of individual lightning return strokes. Using an integrated set of numerical models and directly observed rocket-triggered lightning channel-base currents we calculate the latitudinal dependence of the precipitation signature. Model results indicate that rocket-triggered lightning may produce detectable LEP events and that return strokes with higher ELF (3 Hz–3 kHz) content cause proportionally more ionospheric ionization and precipitate more electrons at higher latitudes than return strokes with proportionally higher VLF (3 kHz–30 kHz) content. The predicted spatio-temporal signature of the induced electron precipitation is highly dependent upon the return stroke spectral content. As a result, we postulate that rocket-triggered lightning experiments enable us to estimate the spectral profile of energetic electrons precipitated from the Earth’s radiation belts. Citation: Cotts, B. R. T., M. Gołkowski, and R. C. Moore (2011), Ionospheric effects of whistler waves from rocket-triggered lightning, Geophys. Res. Lett., 38, L24805, doi:10.1029/2011GL049869.

1. Introduction

One of the dominant natural loss mechanisms for energetic radiation belt electrons in the range $2 < L < 3$ is the electron interaction with lightning-generated whistler mode waves [Abel and Thorne, 1998]. Understanding the removal of these electrons has received significant attention in the past [e.g., Thomson and Dowden, 1977; Yip et al., 1991; Johnson et al., 1999; Clilverd et al., 2002; Peter and Inan, 2007] due to the fact that the on-board electronics of spacecraft are damaged by these high energy fluxes and are particularly vulnerable during periods of enhanced geomagnetic activity [Baker et al., 2004]. In addition, the deposition of energy within the ionosphere by electrons that are precipitated (i.e., removed) from the radiation belts can significantly affect the propagation of subionospheric VLF transmitter signals, potentially reducing the amount of received power by $>3$ dB for several minutes or more [e.g., Inan et al., 1988; Sampath et al., 2000; Peter et al., 2006]. These VLF scattering observations are commonly referred to as lightning-induced electron precipitation (LEP) events.

Much of the previous work has investigated the effects of lightning peak current on electron precipitation. Lauben et al. [2001] showed that the magnitude of pitch angle scattering (and hence the number of precipitating electrons) is linearly related to the magnitude of the lightning-launched electric field. Peter and Inan [2007] demonstrated that it is possible to estimate the number and total energy of precipitating electrons from an observed change in the received amplitude of subionospherically propagating VLF transmitter signals passing through the precipitation region. While it is widely accepted that the frequency content of the lightning source can have a significant effect on the characteristics of LEP events, few studies have focused on quantifying these effects. All previous investigations that address the source lightning spectrum assume a theoretical form for the source lightning frequency content, and none have considered the effects of varying the source frequency content. Moreover, previous works have relied on simple local loss cone calculations and have not included the effect of atmospheric backscatter as described by Cotts et al. [2011]. For example, Chang and Inan [1985] investigated the precipitation at a single location due to an assumed Gaussian-shaped lightning spectrum with a peak at 5 kHz, while Inan et al. [1988] investigated the $L$-dependence of precipitation for a whistler-mode wave with constant intensity between 0.2 kHz and 6 kHz. Rodger et al. [2003] investigated the difference in LEP event recovery for two different assumed electron precipitation spectra (affected both by geomagnetic conditions and source lightning frequency content). While Albert [2001] investigated the diffusion coefficient of electrons of various pitch angles and as a function of whistler frequency (a key component in the LEP process), there has been no systematic analysis on the role of lightning spectral content on the characteristics of LEP events.

The difficulty in calculating the dependence of LEP on source lightning frequency content lies in accurately determining the latter. We address this problem by investigating the geographic precipitation pattern for rocket-triggered lightning flashes at the International Center for Lightning Research and Testing (ICLRT) at Camp Blanding, Florida where the lightning channel-base current is directly measured. Wave particle interaction simulations driven by these rocket-triggered lightning measurements provide a unique opportunity for investigating the potential effects of source lightning spectrum on radiation belt electron loss. Using directly-measured lightning return stroke currents we demonstrate for the first time that the variety of spectra radiated by rocket-
triggered lightning produce a measurable difference in the signature of LEP events. To facilitate comparison with past work, Section 2 discusses analytical estimates of the source lightning content while Section 3 discusses the effects of specific observations of rocket-triggered lightning-flashes.

2. Theoretical Source Lightning Spectrum

[5] An analytical waveform which has received widespread use in past work is that of a double-exponential [Bruce and Golde, 1941], given in equation (1) with several examples shown in Figure 1a. This simple analytical form reflects the characteristics of a typical lightning return stroke reasonably well and allows straightforward spectral analysis. A more realistic model was later introduced, containing an extra rise-time term [Dennis and Pierce, 1964] as shown in equation (2). Model results characterizing the LEP events produced by these two analytical waveforms will be compared with those produced by rocket-triggered triggered.

\[ I(t) = I_0(e^{-at} - e^{-bt}) \]  
\[ I(t) = I_0 \frac{v_0}{\gamma}(e^{-at} - e^{-bt})(1 - e^{-\gamma t}) \]  

[6] In the above equations, \( I_0 \) is a model scaling factor for the peak current, and \( a, b, \gamma, \) and \( v_0 \) are model parameters controlling the rise- and decay-time of the current waveform. Note that as in past work \( I_0 \) is defined in Amperes in equation (1) and in kilo-Amperes in equation (2). The electric field due to a vertical lightning return stroke observed at location \( R, \xi \) is given by Uman [1984, p. 127] as:

\[ E = \frac{\mu_0 h_0 \sin \xi}{2\pi R} \frac{df}{dt}, \]  
where \( R \) is the distance from the source to the observation point (determined as by Lauben et al. [2001]), \( \xi \) is angle of the wave with respect to local zenith and \( h_0 \) is the height of the initial charge (assumed to be 5 km). Substituting equations (1) or (2) into equation (3) yields the far-field power spectral density (PSD), \( S(\omega) \):

\[ S_1(\omega) = K_0 \frac{\omega^2(a - b)^2}{(\omega^2 + a^2)(\omega^2 + b^2)} \]  
\[ S_2(\omega) = K_0 \left( \frac{v_0}{\gamma} \right)^2 \frac{(\delta^2 + 4\omega^2)(\alpha^2\omega - b^2\omega)^2}{(a^2 + \omega^2)(b^2 + \omega^2)(\alpha^2 + \omega^2)(\beta^2 + \omega^2)} \]  

where \( K_0 \) includes all physical constants:

\[ K_0 = \frac{1}{Z_0} \left( \frac{\mu_0 I_0}{2\pi} \right) \left( \frac{\sin \xi}{R} \right)^2, \]  
and \( \alpha = a + \gamma, \ \beta = b + \gamma, \ \delta = a + b + \gamma \).

\( S(\omega) \) is in units of \( \text{Wm}^{-2} \text{Hz}^{-1} \), \( \omega \) is the radial frequency in rad/sec, and \( Z_0 \) and \( \mu_0 \) are the intrinsic impedance (~377 \( \Omega \)) and permeability \((4\pi \times 10^{-7} \ \text{H/m})\) of free space, respectively.

[7] We first vary the parameters of the analytical source lightning spectrum and illustrate the effect on LEP production. Varying the model parameters as shown in Table 1, yields the three waveforms shown in Figure 1a. Each waveform has been chosen to reflect the same peak current (~10 kA) as a typical rocket-triggered return stroke [Nag et al., 2011], but with a peak in the PSD at varying frequencies as shown in Figure 1b. Waveform A1 represents a typical lightning flash with a peak in the PSD at ~10 kHz [Uman, 2001, p. 118], while Waveforms A2 and A3 exhibit PSD maxima at frequencies of ~7.5 kHz and ~3.5 kHz, respectively.

[8] Following the methodology of Bortnik et al. [2006], we use the Whistler-Induced Particle Precipitation (WIPP) code to calculate the magnitude of electron pitch angle scattering at each \( L \)-shell as a function of time and electron energy for each of the waveforms in Figure 1a. The lightning location for each of these simulations is the ICLRT with geographic coordinates of 30°N, 278°E (40°N, 350°E geomagnetic). Using the calculated pitch angle change over the first two seconds of precipitation we then calculate the altitude profile of the ionospheric deposition. Cotts et al. [2011] demonstrated that precipitating electrons backscatter from the atmosphere and are subsequently incident on the conjugate atmosphere. This process can repeat many times, creating ionization with each atmospheric interaction, but the first two depositions are dominant at this longitude. Figure 2a shows an example of secondary ionization for the first two deposition profiles (dashed lines) in the Northern Hemisphere.

Table 1. Lightning Model Parameters as Described in the Text

<table>
<thead>
<tr>
<th>Waveform</th>
<th>( I_0 ) (kA)</th>
<th>a</th>
<th>b</th>
<th>( \gamma )</th>
<th>( v_0 ) (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A1</td>
<td>41.7</td>
<td>5 \times 10^4</td>
<td>1 \times 10^5</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>A2</td>
<td>41.7</td>
<td>5 \times 10^4</td>
<td>1 \times 10^5</td>
<td>3 \times 10^3</td>
<td>5.0 \times 10^7</td>
</tr>
<tr>
<td>A3</td>
<td>19.5</td>
<td>1 \times 10^4</td>
<td>5 \times 10^4</td>
<td>—</td>
<td>—</td>
</tr>
</tbody>
</table>
as well as the sum total of the two curves shown in the solid line.

[9] In order to track the electron resonance dynamics at $L < 2$ we include electrons energies up to 1 MeV. The peak deposition magnitude in the solid black curve in Figure 2a is a quantitative measure representing the precipitation signature at a particular location. This calculation is repeated for each of the analytical waveforms $A_1 - A_3$ with results shown in Figure 3a. The results show that not only does the lightning spectral content influence the LEP signature, but it also significantly determines which regions of the magnetosphere are primarily affected. The lightning return strokes with relatively higher ELF frequency content create a peak in precipitated flux at higher $L$-shells than a “typical” lightning stroke (e.g., $T_1$). As shown by Figure 3b, the peak in the precipitation region for waveform $T_3$ is shifted more than 300 km poleward (0.3 $L$) from that of $T_1$. In addition, the total precipitation (summed over all $L$-shells) for all return strokes are within ~10% of each other, despite the fact that waveform $T_3$ has a peak current ≥30% larger than that of either $T_2$ or $T_3$. This indicates that return strokes with stronger ELF components are more efficient at precipitating energetic electrons from the radiation belts. The shift to higher $L$-shell is due to a combination of lower frequency whistler waves propagating to higher $L$-shells [e.g., Bortnik et al., 2003] and to a decreasing electron cyclotron frequency with increasing $L$. While the former primarily shifts the precipitation region poleward, the latter shifts the resonant energy of electrons to lower energies (where there are a larger number of particles) resulting in a higher total precipitated energy flux. For

[11] Three return strokes from a single rocket triggered flash on 29 March 2009 are shown in Figure 1c. While each stroke is qualitatively similar to those shown in Figure 1a, they contain significantly more structure than can be represented by an analytic approximation. This fact is more apparent from the PSD shown in Figure 1d. Triggered stroke $T_1$ is the largest of the three and has a peak current of ~17 kA and a broad spectral peak near 20 kHz. Stroke $T_3$ has a peak current of ~13 kA and a narrower spectral peak near 4.3 kHz. The continuing currents of stroke $T_2$ (peak current of ~12 kA) produce several narrow spectral peaks, the three largest of which are near 4.0 kHz, 5.5 kHz and 7 kHz, on top of a PSD which decays with frequency more gradually than $T_3$. Calculating the deposition as a function of $L$-shell for the rocket-triggered lightning waveforms yields results similar to those presented in Section 2. As shown in Figure 3b, the peak change in electron density is ~15 elec/cm$^2$, which is only slightly higher than for the analytical (10 kA) waveforms shown in Figure 3a. As shown by Cotts et al. [2011, Figure 9], such electron density changes can produce VLF amplitude changes on the order of 0.2 dB, a change that is detectable in practice, as discussed below.

[12] Figure 3b demonstrates that the lightning PSD significantly alters the regions of the ionosphere and magnetosphere which are most affected by a particular lightning return stroke. For the investigated return strokes, the stroke with the largest ELF content creates a peak in precipitated flux at higher $L$-shells than a “typical” lightning stroke (e.g., $T_1$). As shown by Figure 3b, the peak in the precipitation region for waveform $T_3$ is shifted more than 300 km poleward (0.3 $L$) from that of $T_1$. In addition, the total precipitation (summed over all $L$-shells) for all return strokes are within ~10% of each other, despite the fact that waveform $T_3$ has a peak current ≥30% larger than that of either $T_2$ or $T_3$. This indicates that return strokes with stronger ELF components are more efficient at precipitating energetic electrons from the radiation belts. The shift to higher $L$-shell is due to a combination of lower frequency whistler waves propagating to higher $L$-shells [e.g., Bortnik et al., 2003] and to a decreasing electron cyclotron frequency with increasing $L$. While the former primarily shifts the precipitation region poleward, the latter shifts the resonant energy of electrons to lower energies (where there are a larger number of particles) resulting in a higher total precipitated energy flux. For

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**Figure 2.** (a) Ionospheric electron density enhancement as a function altitude. (b) Example disturbance for waveform $T_3$ with VLF remote-sensing propagation paths.

**Figure 3.** Peak ionospheric electron density enhancement as a function of $L$-shell for (a) analytical lightning waveforms and (b) triggered lightning waveforms.
example, at $L = 2.3$ whistler waves of 0.5–4.5 kHz experience first order resonance with 0.1–1 MeV electrons while at $L = 2.7$ the resonant frequency range for these energies decreases to 0.2–2 kHz. The net result is that 0.1–1 MeV electrons are precipitated only by the ELF frequency components and hence lightning waveforms which have higher PSD at ELF frequencies produce proportionally more ionization. [13] An array of VLF receivers along the eastern coast of the U.S. (e.g., as shown in Figure 2b) can capture this $L$-dependent precipitation signature in a manner very similar to previous work performed in Colorado [e.g., Peter and Inan, 2007]. Such an array, with receivers spaced every 0.1 $L$ ($\sim110$ km), would provide a metric by which future LEP events could be compared. Similarly, an array of VLF receivers (with longitudinal spacing) in the southeastern U.S. may be used to simultaneously quantify the longitudinal extent of the precipitation region. In the absence of a measurement station at every 0.1 $L$, Figure 3b also indicates that it is sufficient to perform observations at only a few locations. The shift in the resultant peak deposition among different source waveforms is large enough (0.3 $L$ or $>300$ km) that the ratio of the deposition at just two separate $L$-shells suffices to differentiate among the precipitation signatures considered here. As shown in Figure 3b the ratio of the peak deposition at $L = 2.3$ and the peak deposition at $L = 2.7$ for lightning waveforms $T_1$, $T_2$ and $T_3$ is $1.3$, $0.9$ and $0.6$, respectively. Past observations of LEP events using VLF remote sensing [Peter and Inan, 2007] have demonstrated the ability to quantify LEP induced amplitude changes of less than 0.1 dB and experimental differentiation between observed ratios at least ten percent above or below unity is feasible using VLF remote sensing. The predicted ratios described in Figures 3b and 4b are therefore well within observable limits of VLF remote sensing experiments.

4. Conclusions

[15] The results described in Sections 2 and 3 indicate that differences in the causative lightning spectrum produce measurable differences in the $L$-dependent magnitude of LEP events. The precise lightning return stroke frequency content obtained from rocket-triggered measurements combined with a forward modeling numerical approach can provide an estimate not only of the total precipitated energy flux, but also a measure of the spectral profile of precipitating electrons. Rocket-triggered lightning thus allows for the controlled investigation of the LEP phenomena and greater understanding of the removal of energetic radiation belt electrons by lightning as well as quantification of the effect that precipitating electrons have on the subionospheric communication channel.

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References


Bortnik, J., U. S. Inan, and T. F. Bell (2006), Temporal signatures of radiation belt electron precipitation induced by lightning-generated MR whistler waves it also affect the L-dependence of LEP. To show the effect of disturbed geomagnetic conditions (disturbed conditions also influence the magnitude of observed LEP events [Peter et al., 2006]) we model the same three triggered lightning strokes in Figure 1c using the disturbed profile represented by the dashed line of Figure 4a. The results are shown in Figure 4b where it is clear that the plasmapause at $L \approx 3$ has a significant guiding-effect on the trajectory of the whistler waves resulting in very little precipitation outside this region. As a result of this guiding effect, the L-dependent precipitation signature tends to be slightly broader with a sharper drop-off when compared to the quiet conditions (Figure 3b). However, the L-dependence of the precipitation region seen in quiet geomagnetic conditions still holds. For this case the ratio of peak deposition at $L = 2.3$ and $L = 2.7$ for lightning waveforms $T_1$, $T_2$ and $T_3$ is $1.3$, $0.9$ and $0.6$, respectively. Past observations of LEP events using VLF remote sensing [Peter and Inan, 2007] have demonstrated the ability to quantify LEP induced amplitude changes of less than 0.1 dB and experimental differentiation between observed ratios at least ten percent above or below unity is feasible using VLF remote sensing. The predicted ratios described in Figures 3b and 4b are therefore well within observable limits of VLF remote sensing experiments.

Figure 4. (a) Magnetospheric electron density profiles used in simulations. (b) Peak precipitation vs. $L$-shell using a disturbed magnetosphere.
Uman, M. A. (2001), The Lightning Discharge, Dover, Mineola, N. Y.

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